

# Mathematics Benchmarking Report TIMSS 1999 – Eighth Grade

Achievement for U.S. States and Districts in an International Context

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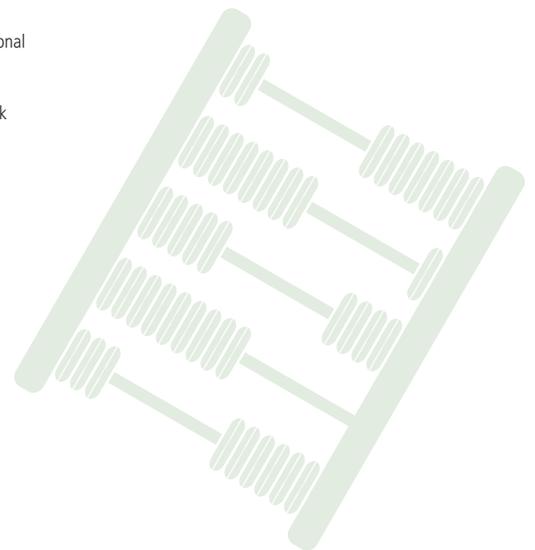
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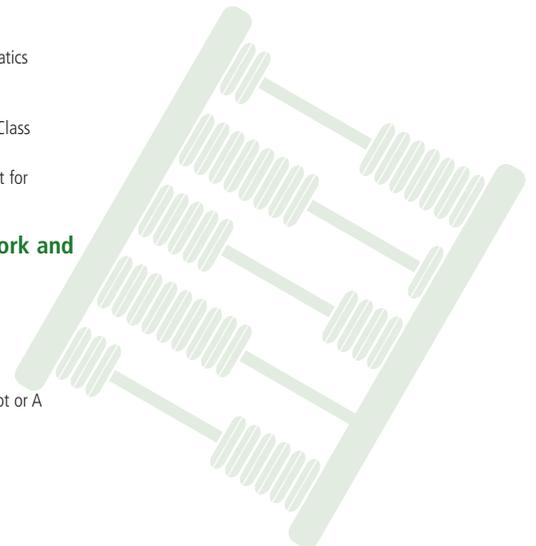
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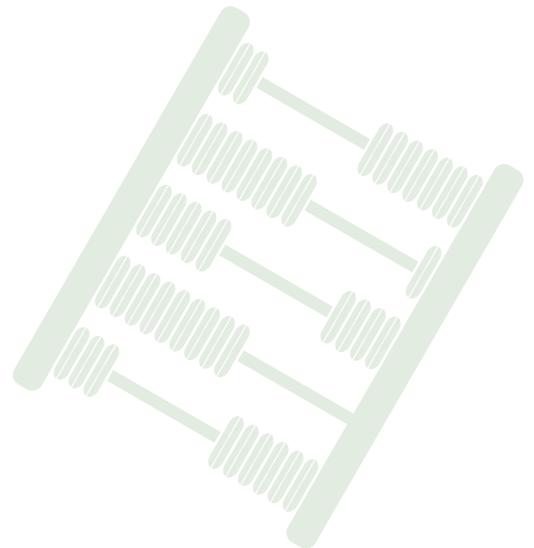
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